	Diploma Programme subject	outline-Group 5: mathem	atics	
School name	Gymnázium, Šrobárova 1, Košíce, Slovakia		School code	061626
Name of the DP subject	DP Mathematics: Applications and Interpretation	DP Mathematics: Applications and Interpretation		
(indicate language)				
Level (indicate with X)	Higher X Standard	completed in two years X Standard	d completed in one	year*
Name of the teacher who completed this outline	Katarína Hribová	Date of IB training	3 February – 3	March 2021
Date when outline was completed	28 June 2021	Name of workshop (indicate name of subject and workshop category)	Mathematics: A Interpretation (Applications and (Cat.1)

1. Course outline

- Use the following table to organize the topics to be taught in the course. If you need to include topics that cover other requirements you have to teach (for example, national syllabus), make sure that you do so in an integrated way, but also differentiate them using italics. Add as many rows as you need.
- This document should not be a day-by-day accounting of each unit. It is an outline showing how you will distribute the topics and the time to ensure that students are prepared to comply with the requirements of the subject.
- This outline should show how you will develop the teaching of the subject. It should reflect the individual nature of the course in your classroom and should not just be a "copy and paste" from the subject guide.
- If you will teach both higher and standard level, make sure that this is clearly identified in your outline.

^{*} All Diploma Programme courses are designed as two-year learning experiences. However, up to two standard level subjects, excluding languages ab initio and pilot subjects, can be completed in one year, according to conditions established in the *Handbook of procedures for the Diploma Programme*.

	Topic/unit (as identified in the IB subject guide) State the topics/units in the order you are planning to teach them.	Contents	One class is 45 minutes.	Assessment instruments to be used	Resources List the main resources to be used, including information technology if applicable.
Year 1	Topic 1: Number and Algebra	SL and HL common content SL 1.1 Operations with numbers in the form $a \times 10^k$ where $1 \le a < 10$ and k is an integer SL 1.2 -Arithmetic sequences and series SL 1.3 -Geometric sequences and series SL 1.4 -Financial applications of geometric sequences and series: compound interest, annual depreciation SL 1.5 -Laws of exponents with integer exponents -Introduction to logarithms with base 10 and e SL 1.6 -Approximation -Upper and lower bounds of rounded numbers -Percentage errors -Estimation SL 1.7 -Amortization and annuities using technology SL 1.8 Use technology to solve: -Systems of linear equations in up to 3 variables -Polynomial equations	In one week there are SL: 4 HL:6 Recommended teaching hours: SL: 16 hours (21 classes) HL: 29 hours (39 classes)	students' ability to apply what they have learned in mathematics to real-world contexts. Students will be expected to demonstrate the following: -knowledge and understanding -problem solving -communication and interpretation -technology -reasoning -inquiry approaches Assessment: -will take place during the course -discussions	Textbooks: IB Mathematics: Applications and Interpretations SL (OUP) IB Mathematics: Applications and Interpretations HL (OUP) Online resources: https://questionbank.ibo.org/ https://app.kognity.com/ https://www.thinkib.net/mathapplications https://resources.ibo.org/home Software/Technology: GDC Desmos GeoGebra Other software Other resources: YouTube Khan Academy Mathematical Exploration examples IB Question Bank
		Torymormal equations		-homework -short tests -end of topic tests -end of chapter tests	

	HL content		-end of term progress	
	AHL 1.9		check tests	
	-Laws of logarithms		-short Practice IA	
	AHL 1.10			
	-Simplifying expressions, both numerically and		Students will be strongly	
	algebraically, involving rational expressions		encouraged to self-	
	AHL 1.11		assess throughout the	
	-The sum of infinite geometric sequences		=	
	AHL 1.12		course.	
	-Complex numbers			
	AHL 1.13		Grade descriptors 7-1:	
	-Modulus-argument polar form:		See document DP Grade	
	$z = r(\cos\theta + i\sin\theta)$		Descriptors, p.16-17	
	-Exponential form:			
	$z = re^{i\theta}$		Also, see the school	
	AHL 1.14		Assessment policy	
	-Matrices		' '	
	AHL 1.15			
	-Eigenvalues and eigenvectors			
	-2×2 matrices			
Topic 2:	SL and HL common content	Recommended teaching		
Functions	SL 2.1	hours:		
	-Equation of a straight line			
	-Gradients; intercepts	SL: 31 hours		
	SL 2.2	(41 classes)		
	-Function	(41 Classes)		
	SL 2.3	42.1		
	-The graph of a function	HL: 42 hours		
	SL 2.4	(56 classes)		
	-Key features in graphs			
	-Point of intersection of two curves or lines			
	using technology			
	SL 2.5			
	Modelling with the following functions:			
	-Linear models			
	-Quadratic models			
	-Exponential growth and decay models			
	-Direct/inverse variation			
	-Cubic models			
	-Sinusoidal models			
	SL 2.6			
	Modelling skills		1	

HL content AHL 2.7 -Composite functions -Inverse functions -Inverse functions AHL 2.8 -Transformation of graphs -Translations -Reflections in the x-axis and in the y-axis -Vertical stretch -Horizontal stretch -Horizontal stretch -Composite transformations AHL 2.9 Modelling with the following functions: 1.Exponential models to calculate half-life 2. Natural logarithmic models 3.Sinusoidal models 4.Logistic models 5.Piecewise models AHL 2.10 -Scaling very large or small numbers using logarithms -Linearizing data using logarithms or a power relationship SL and HL common content SL 3.1 -The distance between two points in three dimensional solids including right-pyramid, right-cone, sphere, hemisphere and combination of these solids -The size of an angle between two interjecting lines or between a line and a plane SL 3.2 -Use of sine, cosine and tangent ratios to find the sides and angles of right-angled triangles HL 46 hours (61 classes)
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-Inverse functions AHL 2.8 -Transformation of graphs -Translations Reflections in the x-axis and in the y-axis -Vertical stretch -Horizontal stretch -Composite transformations AHL 2.9 Modelling with the following functions: 1.Exponential models to calculate half-life 2.Natural logarithmic models 3.Sinusoidal models 4.Logistic models 5.Piecewise models AHL 2.10 -Scaling very large or small numbers using logarithms -Linearizing data using logarithms or a power relationship SL and HL common content SL 3.1 -The distance between two points in three dimensional solids including right-pyramid, right-cone, sphere, hemisphere and combination of these solids -The size of an angle between two interjecting lines or between a line and a plane SL 3.2 -Use of sine, cosine and tangent ratios to find the sides and angles of right-angled triangles HL: 46 hours (61 classes)
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SL 3.2 -Use of sine, cosine and tangent ratios to find the sides and angles of right-angled triangles HL: 46 hours (61 classes)
-Use of sine, cosine and tangent ratios to find the sides and angles of right-angled triangles (61 classes)
the sides and angles of right-angled triangles
- The sine rule
-The cosine rule
-Area of a triangle

SL 3.3
-Applications of right and non-right angled
trigonometry, including Pythagoras´ theorem
-Angles of elevation and depression
SL 3.4
-The circle: length of an arc; area of a sector
SL 3.5
-Equations of perpendicular bisectors
SL 3.6
-Voronoi diagrams
-Nearest neighbour interpolation
-Application of the "toxic waste dump"
problem
HL content
AHL 3.7
-The definition of a radian and conversion
between degrees and radians
-Using radians to calculate area of sector,
length of arc
AHL 3.8
-The definitions of $\cos \theta$ and $\sin \theta$ in terms of
the unit circle
-The Pythagorean identity
-Definition of $ an heta$
-Extension of the sine rule to the ambiguous
case
-Graphical methods of solving trigonometric
equations in a finite interval
AHL 3.9
-Geometric transformations of points in two
dimensions using matrices
-Geometric interpretations of the determinant
of a transformation matrix
AHL 3.10
-Vectors and scalars
AHL 3.11
-Vector equation of a line in 2D and 3D
AHL 3.12
-Vector applications to kinematics
-Modelling linear motion
Modelling linear motion

	AHL 3.13		
	-Scalar product of two vectors		
	-The angle between two vectors; the acute		
	angle between two lines		
	-Vector product of two vectors		
	-Geometric interpretation of $ v \times w $		
	AHL 3.14		
	-Graph theory		
	-Simple graphs; complete graphs; weigted		
	graphs		
	-Directed graphs		
	-Subgraphs; trees		
	AHL 3.15		
	-Adjacency matrices		
	-Walks		
	-Weighted adjacency tables		
	-Construction of the transition matrix for a		
	strongly-connected, undirected or directed		
	graph		
	AHL 3.16		
	-Tree and cycle algorithms with undirected		
	graphs		
	-Walks, trails, paths, circuits, cycles		
	-Eulerian trails and circuits		
	-Hamiltonian paths and cycles		
	-Minimum spanning tree (MST) graph		
	algorithms		
	-Kruskal's and Prim's algorithms		
	-Chinese postman problem and algorithm -Travelling salesman probem to determine the		
	Hamiltonian cycle of least weight in a weighted		
	complete graph		
	-Nearest neighbour algorithm		
	-Deleted vertex algorithm		
	Deleted vertex digoritimi		
Introduction to	SL and HL	Pacammandad taashisa	
Introduction to	-Discuss what the Internal Assessment is,	Recommended teaching	
	the criteria for grading, academic honesty,	hours:	
	<u> </u>	SL/HL: 10 hours	
	samples, possible topics	(SL/HL: 13 classes)	
	-Practice Al		
		(SL: 8 classes)	
Revision	-Past paper questions practice	(HL: 4 classes)	
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Year 1	Topic 4:	SL and HL common content	Recommended teaching	Assessment revolves	Textbooks:
&	Statistics and Probability	St 4.1	hours:	around evaluating	IB Mathematics: Applications and
Year 2		-Concepts of population, sample, random			Interpretations SL (OUP)
I Gal Z		sample, discrete and contiuous data -Reliability of data source and bias in sampling	SL: 16 + 20 hours	· ·	IB Mathematics: Applications and
		-Interpretation of outliers	(21 + 27 classes)	in mathematics to real-	Interpretations HL (OUP)
		-Sampling techniques and their effectiveness		world contexts.	
		SL 4.2	HL: 14 + 38 hours		Online resources:
		-Presentation of data (discrete and	(19 + 50 classes)	Students will be	https://questionbank.ibo.org/
		continuous):frequency distributions (table)	,	expected to	https://app.kognity.com/
		-Histograms		demonstrate the	•https://www.thinkib.net/mathapplications
		-Cumulative frequency graphs		following:	https://resources.ibo.org/home
		-Box and whisker diagrams		-knowledge and	
		SL 4.3		understanding	Software/Technology:
		-Measures of central tendency		_	• GDC
		-Estimation of mean from grouped data		-problem solving	• Desmos
		-Modal class		-communication and	GeoGebra
		-Measures of dispersion		interpretation	Other software
		-Effect of constant changes to the original data		-technology	
		-Quartiles of discrete data		-reasoning	Other resources:
		SL 4.4		-inquiry approaches	• YouTube
		-Linear correlation of bivariate data			Khan Academy
		-Pearson's product-moment correlation		Assessment:	•
		coefficient r		-will take place during	Mathematical Exploration examples In Overtical Parks
		-Scatter diagrams; lines of best fit		the course	IB Question Bank
		-Equation of the regression line of y on x		-discussions	
		SL 4.5		-homework	Other resources:
		-Concepts of trial, outcome, equally likely		-short tests	• YouTube
		outcomes, relative frequency, sample space		-end of topic tests	Khan Academy
		(U) and event		-end of chapter tests	Mathematical Exploration examples
		-The probability of an event <i>A</i>		- end of term progress	IB Question Bank
		-The complementary events <i>A</i> , <i>A</i> ′ -Expected numbers of occurences		check tests	
		SL 4.6		CHECK LESTS	
		-Venn diagrams, tree diagrams, sample space		Final IA (tha)	
		diagrams and tables of outcomes		-Final IA (tbc)	
		-Combined events		-Final Exam (May)	
		-Mutually exclusive events			
		-Conditional probability		Students will be strongly	
		-Independent events		encouraged to self-	
				assess throughout the	
				course.	

SL 4.7

-Discrete random variables and their probability distributions

-Expected value (mean), E(X) for discrete data

SL 4.8

-Binomial distribution

SL 4.9

-The normal distribution and curve
-Normal probability representations

-Inverse normal calculations

SI 4.10

-Spearman's rank correlation coefficient
-Awareness of the apropriateness and
limitations of Pearson's product moment
correlation coefficient and Spearman's rank
correlation coefficient, and the effect of
outliers on each

SL 4.11

-Formulation of null and alternative hypotheses

-Significant levels

-p-values

-Expected and observed frequences

-The χ^2 test for independence: contingency tables, degree of freedom, critial value

-The χ^2 goodness of fit test

-The *t*-test

-Use of the p-value to compare the means of two populations

-Using one-tailed and two-tailed tests

HL content

AHL 4.12

-Data collection methods: surveys and questionnaires

-Selecting relevant variables from many variables

-Chosing relevant and appropriate data to analyse

-Categorising numerical data in a χ^2 table -Reliability and validity + tests

IA Assessment criteria:

A – Presentation

B – Mathematical

communication

C – Personal

Engagement

D – Reflection

E – Use of Mathematics

Final Exam and

Assessment outline (SL):

-External

Paper 1, 90 min., 40%

Paper 2, 90 min., 40%

-Internal

Mathematical

Exploration, 20%

Final Exam and

Assessment outline (HL):

-External

Paper 1, 120 min., 30%

Paper 2, 120 min., 30%

Paper 3, 60 min., 20%

-Internal

Mathematical

Exploration, 20%

Grade descriptors 7-1: See document DP Grade

Descriptors, p.16-17

Also, see the school Assessment policy

ANL 4.13 Non-linear regression -Evaluating of least squares regression curves using technology Sum of square residuals (SS _{reg}) -The coefficient of determination (R²) ANL 4.14 Linear transformation of a single random variable -Expected value of linear combinations of π random variables -Variance of linear combinations of π independent random variables - π as an unbiased estimate of μ - π - π - π - π - π - π - π - π - π - π				
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AHL 4.19				
-Transition matrices				
-Regular Markov chains		_		
-Initial state probability matrices				
-Steady state and long-term probabilities	-St	eady state and long-term probabilities		

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Year 2	Topics 5:	SL and HL common content	Recommended teaching		
	Calculus	SL 5.1	hours:		
		-Introduction to the concept of a limit			
		-Derivative interpreted as gradient function	SL: 19 hours		
		and as rate of change	(26 classes)		
		SL 5.2	(20 classes)		
		-Increasing and decreasing functions			
		-Graphical interpretation of	HL: 41 hours		
		f'(x) > 0, f'(x) = 0, f'(x) < 0	(55 classes)		
		SL 5.3			
		-Derivative of $f(x) = ax^n$ is			
		$f'(x) = anx^{n-1}, n \in \mathbb{Z}$			
		-The derivative of functions in the form			
		$f(x) = ax^n + bx^{n-1} + \cdots$ where all exponents			
		are integers			
		SL 5.4			
		-Tangents and normals			
		SL 5.5			
		-Introduction to the integration as anti-			
		differentiation of functions of the form			
		$f(x) = ax^n + bx^{n-1} + \cdots$, where			
		$n \in \mathbb{Z}, n \neq -1$			
		$n \in \mathbb{Z}, n \neq -1$ -Anti-differentiation with a bundary condition			
		to determine the constant term			
		-Definite integrals using technology -Area of a region enclosed by a curve $y = f(x)$			
		and the x -axis, where $f(x) > 0$			
		SL 5.6			
		-Values of x where the gradient of a curve is			
		zero			
		-Solution of $f'(x) = 0$			
		-Local maximum and minimum points			
		SL 5.7			
		-Optimisation problems in context			
		SL 5.8			
		-Trapezoidal rule			

HL content	
AHL 5.9	
-The derivatives of $\sin x$, $\cos x$, $\tan x$,	
e^x , $\ln x$, x^n , where $n \in \mathbb{Q}$	
-The chain rule, product and quotient rules	
-Related rates of change	
AHL 5.10	
-The second derivative	
-Use the second derivative test to distinguish	
between a maximum and a minimum point	
AHL 5.11	
-Definite and indefinite integration of $oldsymbol{x}^n$	
where $n \in \mathbb{Q}$, including $n = -1$, $\sin x$, $\cos x$,	
$\frac{1}{\cos^2 x}$ and e^x	
cos^2x -Integration by inspection, or substitution of	
the form $\int f(g(x))g'(x)dx$	
AHL 5.12	
-Area of the region enclosed by a curve and the	
x or the y-axes ina given interval	
-Volumes of revolution about the x -axis or y -	
axis	
AHL 5.13	
-Kinematic problems involving displacement <i>s</i> ,	
velocity v and acceleration a	
AHL 5.14	
-Setting up a model/differential equation from	
context	
-Solving by separation of variables	
AHL 5.15	
-Slope fields and their diagrams	
AHL 5.16	
-Euler's method for finding the approximate	
solution to first order differential equations	
-Numerical solution of $\frac{dy}{dx} = f(x, y)$	
-Numerical solutions of the coupled system	
$\frac{dx}{dt} = f_1(x, y, t)$ and $\frac{dy}{dt} = f_2(x, y, t)$	
dt dt dt	

	Phase portrait for the solutions of coupled differential equations of the form: $\frac{dx}{dt} = ax + by; \frac{dy}{dt} = cx + dy$ -Qualitative analysis of future paths for distinct, real, complex and imaginary eigenvalues -Sketching trajectories and using phase portraits to identify key features such as equilibrium points, stable populations and saddle points. AHL 5.18 -Solutions of $\frac{d^2x}{dt^2} = f(x, \frac{dx}{dt}, t)$ by Euler's method				
Final Mathematical Exploration	SL and HL -Completing the final Mathematical Exploration IA	Recommended teaching hours: SL/HL: 20 hours (SL/HL: 27 classes)			
Exam Revision and Preparation	-In preparation for the final exams, students will revise using past paper questions, past papers and past assignments	(SL: 12 classes) (HL: 6 classes)			
	Exploration Exam Revision and	-Phase portrait for the solutions of coupled differential equations of the form: $\frac{dx}{dt} = ax + by; \frac{dy}{dt} = cx + dy$ -Qualitative analysis of future paths for distinct, real, complex and imaginary eigenvalues -Sketching trajectories and using phase portraits to identify key features such as equilibrium points, stable populations and saddle points. AHL 5.18 -Solutions of $\frac{d^2x}{dt^2} = f(x, \frac{dx}{dt}, t)$ by Euler's method $\frac{\text{SL and HL}}{\text{Exam Revision and Preparation}}$ -In preparation for the final Mathematical Exploration in past paper questions, past papers and past	-Phase portrait for the solutions of coupled differential equations of the form: $\frac{dx}{dt} = ax + by; \frac{dy}{dt} = cx + dy$ -Qualitative analysis of future paths for distinct, real, complex and imaginary eigenvalues -Sketching trajectories and using phase portraits to identify key features such as equilibrium points, stable populations and saddle points. AHL 5.18 -Solutions of $\frac{d^2x}{dt^2} = f(x, \frac{dx}{dt}, t)$ by Euler's method Final Mathematical Exploration SL and HL -Completing the final Mathematical Exploration IA Final Revision and Preparation -In preparation for the final exams, students will revise using past paper questions, past papers and past (SL: 12 classes) (SL: 12 classes)	-Phase portrait for the solutions of coupled differential equations of the form: $\frac{dx}{dt} = ax + by; \frac{dy}{dt} = cx + dy$ -Qualitative analysis of future paths for distinct, real, complex and imaginary eigenvalues -Sketching trajectories and using phase portraits to identify key features such as equilibrium points, stable populations and saddle points. AHL 5.18 -Solutions of $\frac{d^2x}{dt^2} = f(x, \frac{dx}{dt}, t)$ by Euler's method Final Mathematical Exploration SL and HL -Completing the final Mathematical Exploration IA SL 20 hours (SL/HL: 20 hours (SL/HL: 27 classes) Exam Revision and Preparation -In preparation for the final exams, students will revise using past paper questions, past papers and past	-Phase portrait for the solutions of coupled differential equations of the form: $\frac{dx}{dt} = ax + by; \frac{dy}{dt} = cx + dy$ -Qualitative analysis of future paths for distinct, real, complex and imaginary eigenvalues -Sketching trajectories and using phase portraits to identify key features such as equilibrium points, stable populations and saddle points. AHL 5.18 -Solutions of $\frac{d^2x}{dt^2} = f(x, \frac{dx}{dt}, t)$ by Euler's method Final Mathematical Exploration SL and HL -Completing the final Mathematical Exploration IA Final Mathematical Exploration of The final Exploration of The Fi

2. IB internal assessment requirement to be completed during the course

Briefly explain how and when you will work on it. Include the date when you will first introduce the internal assessment requirement to your students, the different stages and when the internal assessment requirement will be due.

The internal assessment (IA) is an individual exploration. This is a piece of written work that involves investigating an area of mathematics.

- Students willl be introduced to Mathematical Exploration during the second term of Year f 1
- Students will do a short practice Mathematical Exploration Internal Assessment in Year 1 (6-8 pages)
- Students willl continue to work on their Mathematical Exploration during Year 2
- Students are expected to complete their Final Mathematical Exploration Internal Assessment in Year 2 (deadline: see school calendar)

3. Links to TOK

You are expected to explore links between the topics of your subject and TOK. As an example of how you would do this, choose one topic from your course outline that would allow your students to make links with TOK. Describe how you would plan the lesson.

Topic	Link with TOK (including description of lesson plan)
Topic 1: Number and Algebra	TOK: Is all knowledge concerned with identification and use of patterns? Consider Fibonacci numbers and connections with the
SL 1.2 Arithmetic sequences	Golden ratio.
and series	Aim: Explore knowledge via the perspectives + methods and tools elements in mathematics from the TOK curriculum, considering
	Fibonacci numbers and connections with the Golden ratio. (Note: The lesson follows cooperative planning with the ToK teacher.)
	Activity: Students will look at how mathematics often appears in nature. They will start by recalling Fibonacci numbers and their
	sequence. Then students will be presented with some pictures to explore the Golden ratio (pair/group work). They will present
	their findings to the rest of the class. Connections will be drawn between the Fibonacci numbers and the Golden ratio. Students
	will find their own examples and think of other possible applications.

4. Approaches to learning

Every IB course should contribute to the development of students' approaches to learning skills. As an example of how you would do this, choose one topic from your outline that would allow your students to specifically develop one or more of these skill categories (thinking, communication, social, self-management or research).

Topic	Contribution to the development of students' approaches to learning skills (including one or more skill category)
Topic 4: Statistics and	Students will choose a research topic of their interest, design a questionnaire and conduct their own survey (among
Probability	their peers, family members, members of the public,). After collecting their data, they will analyse it, present it
AHL 4.12 Data collection	graphically and draw conclusions. They will make a short presentation about their research to their classmates and
methods: surveys and	answer their questions.
questionnaires	
SL 4.1 – SL 4.4 or other	

5. International mindedness

Every IB course should contribute to the development of international-mindedness in students. As an example of how you would do this, choose one topic from your outline that would allow your students to analyse it from different cultural perspectives. Briefly explain the reason for your choice and what resources you will use to achieve this goal.

Topic	Contribution to the development of international mindedness (including resources you will use)
Topic 5: Calculus SL 5.1 Introduction to the	International-mindedness: Attempts by Indian mathematicians (500-1000 CE) to explain division by zero.
concept of a limit	Students will explore the history and origin of zero, operations with zero and the connection with the concept of a limit. e.g. You Tube video: The story of zero – getting something from nothing; The Royal Institution https://aeon.co/videos/a-history-of-nothing-how-zero-went-from-nil-to-something Other resources will include various websites and books about the history of mathematics.
	Reason for choice: Zero is a fascinating concept and nowadays we take it for granted. I think it is important for students to see how the concept of zero developed and how it was perceived and used in different cultures.

5. Development of the IB learner profile

Through the course it is also expected that students will develop the attributes of the IB learner profile. As an example of how you would do this, choose one topic from your course outline and explain how the contents and related skills would pursue the development of any attribute(s) of the IB learner profile that you will identify.

Торіс	Contribution to the development of the attribute(s) of the IB learner profile				
Topic 3 : Geometry and	Inquirers – Students will look at different types of triangles and ask curious questions about their connection with				
Trigonometry	different trigonometry ratios and rules.				
SL 3.2 Sine, cosine, tangent	Knowledgeable – Students use their understanding of the concepts and explore the application of their knowledge in				
ratios ; Sine rule, Cosine rule,	contexts such as triangulation, map-making and other subjects such as physics.				
Area of triange	Thinkers – Students will work on complex problems applying their knowledge of different trigonometry ratios and rules				
	Communicators – Students will be expected to communicate their ideas individually using correct mathematical wri				
	but also with confidence and collaboratively as a part of a group when working in pairs/groups.				
	Principled – In all areas of this topic, students are expected to sketch well-labelled diagrams to support their solutions				
	and to work out the answers systematically: write down the formula, substitute, calculate, give answer including units				
	Open-minded – Students will learn about the occurrence of Pythagoras'theorem in early Chinese and Indian				
	manuscripts ad the earliest references to trigonomentry in Indian mathematics.				
	Reflective – Students will reflect upon their work, identify misconceptions and seek ways for improvement.				

6. Resources

Describe the resources that you and your student will have to support the subject. Indicate whether they are sufficient in terms of quality, quantity and variety. Briefly describe what plans are in place if changes are needed.

I have come across the following resource suggestions during the IB workshop. Some are free and some require purchase / subscription. Some textbooks will be used for reference and as teacher planning material, some will be used by students as the study material. The school is supportive in purchasing the resources needed and sufficient funds have been allocated.

Textbooks:

- IB Mathematics: Applications and Interpretations SL (OUP)
- IB Mathematics: Applications and Interpretations HL (OUP)
- Mathematics: Applications and Interpretations SL (Pearson)
- Mathematics: Applications and Interpretations HL (Pearson)
- Mathematics for the IB Diploma: Applications and Interpretation SL (Hodder)
- Mathematics for the IB Diploma: Applications and Interpretation HL (Hodder)
- Mathematics Core Topics SL1 (Haese)
- Mathematics Applications and Interpretations SL2 (Haese)
- Mathematics Core Topics HL1 (Haese)
- Mathematics Applications and Interpretations HL2 (Haese)

Online resources:

- https://questionbank.ibo.org/
- https://app.kognity.com/
- https://www.thinkib.net/mathapplications
- https://resources.ibo.org/home

Software/Technology:

- GDC
- Desmos
- GeoGebra
- Other software (Word, Excel, Powerpoint, apps, ...)

Other resources:

- YouTube
- Khan Academy
- Mathematical Exploration examples
- IB Question Bank